

AQA Qualifications

# GCSE

# **Mathematics**

Unit 1 43601H Mark scheme

43601H November 2014

Version 1.1

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from aqa.org.uk

## **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

| М               | Method marks are awarded for a correct method which could lead to a correct answer.  |
|-----------------|--|
| M dep           | A method mark dependent on a previous method mark being awarded.   |
| A               | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| В               | Marks awarded independent of method.   |
| B dep           | A mark that can only be awarded if a previous independent mark has been awarded.   |
| Q               | Marks awarded for Quality of Written Communication.  |
| ft              | Follow through marks. Marks awarded for correct working following a mistake in an earlier step.  |
| SC              | Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.                        |
| oe              | Or equivalent. Accept answers that are equivalent.   |
|                 | eg accept 0.5 as well as $\frac{1}{2}$   |
| [a, b]          | Accept values between a and b inclusive.   |
| 3.14            | Allow answers which begin 3.14 eg 3.14. 3.142, 3.149   |
| Use of brackets | It is not necessary to see the bracketed work to award the marks.  |

#### Examiners should consistently apply the following principles

#### **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

### Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

#### Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

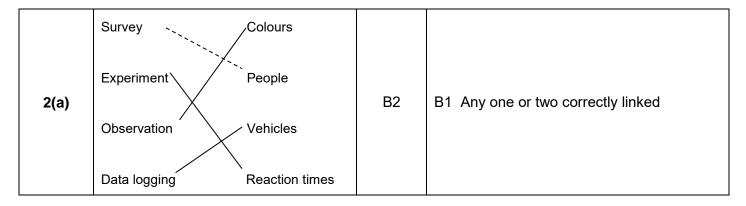
#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### **Premature approximation**

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| Q    | Answer   | Mark | Comments  |  |
|------|--|------|---|--|
|      |  |      |   |  |
| 1(a) | All four points plotted correctly (275, 125), (150, 190), (125, 225), (180, 175)           | B2   | B1 for two or three correct plots   |  |
|      |  |      |   |  |
| 1(b) | Appropriate line of best fit   | B1   | A straight line at least 4 squares wide which goes through, or would go through, the two gates (125, 175 - 225) and (275, 75 - 125) |  |
|      |  |      |   |  |
| 1(c) |  |      | ft their negative, straight line of best fit  |  |
|      | Correct reading from their graph   | B1ft | If B0 awarded in (b), accept answer in range [145, 150]   |  |
|      |  | L    |   |  |
|      | Additional Guidance  |      |   |  |
| 1(c) | Allow ± ½ square tolerance but condone rounding up to the next 5 or down to the previous 5 |      |   |  |



|      | Primary selected <b>and</b><br>Secondary <b>not</b> selected | B1 |  |
|------|--|----|--|
| 2(b) | Discrete selected <b>and</b> Continuous <b>not</b> selected  | B1 |  |

|      | Additional Guidance |    |
|------|---------------------|----|
|      | 1, 3                | B2 |
| 2(b) | 1, 4                | B1 |
| _(2) | 1, 3, 4             | B1 |
|      | 1, 2, 3             | B1 |
|      | 2, 3                | B1 |

All four correct combinations **and** scores (in any order)

3

| W | D | L | Score |
|---|---|---|-------|
| 4 | 0 | 0 | 8     |
| 3 | 1 | 0 | 7     |
| 3 | 0 | 1 | 6     |
| 2 | 2 | 0 | 6     |
| 2 | 1 | 1 | 5     |
| 1 | 3 | 0 | 5     |

B2 for any 2 or 3 correct combinations (condone missing or incorrect scores)

B3 B1 for any 1 correct combination (cond

B1 for any 1 correct combination (condone missing or incorrect score)

Rows may be in any order

|   | Additional Guidance                            |
|---|--|
| 3 | Accept blank as zero                           |
| 3 | Must have correct scores for B3                |
|   | Beware 2, 1, 0 = 5 (doesn't add up to 4 games) |

| 4(a) | Alternative method 1                    |    |                                  |
|------|---|----|----------------------------------|
|      | 3 × 5 or 15 (children) or 20 (children) | M1 | eg 3:15                          |
|      | 15 and 20 and No                        | A1 | oe No, they had 5 extra children |
|      | Alternative method 2                    |    |                                  |
|      | 20 ÷ 5 or 20 (children) or 4 (adults)   | M1 | eg 4:20                          |
|      | 4 and No                                | A1 | oe No, they needed 1 more adult  |

|      | Additional Guidance   |      |  |
|------|---|------|--|
|      | Allow misreads for the other sports on Saturday or walking on Sunday or walking on Saturday and Sunday: |      |  |
| 4(a) | 27 ÷ 5 or 5.4 (adults)  | M1A0 |  |
|      | 18 ÷ 5 or 3.6 (adults)  | M1A0 |  |
|      | 30 ÷ 5 or 6 (adults)  | M1A0 |  |
|      | 50 ÷ 5 or 10 (adults)   | M1A0 |  |

| 4(b) | $\frac{1}{3}$ or $\frac{9}{27}$ or $\frac{8}{24}$ | B1 | oe fraction |
|------|---|----|-------------|
|------|---|----|-------------|

|      | 12 ÷ 3 or<br>30 ÷ 5 or<br>16 ÷ 2   | M1 | 4 adults (archery) or<br>6 adults (walking) or<br>8 adults (sailing)<br>NB 4, 6, 3 implies M0   |
|------|------------------------------------|----|---|
| 4(c) | 12 ÷ 3 and<br>30 ÷ 5 and<br>16 ÷ 2 | M1 | 4 adults (archery) and 6 adults (walking) and 8 adults (sailing)  Condone misread of <b>one</b> bar height if number of adults rounded up |
|      | 18                                 | A1 | Must be from 12, 30 and 16  |

|      | Additional Guidance  |                               |  |  |  |
|------|--|-------------------------------|--|--|--|
|      | Condone all M marks for misread of Saturday for any bar:       |                               |  |  |  |
|      | Archery : 27 ÷ 3 = 9   | M1                            |  |  |  |
|      | Walking : 20 ÷ 5 = 4   |                               |  |  |  |
|      | Sailing : 18 ÷ 2 = 9 (Total = 22)                              | M1A0                          |  |  |  |
| 4(c) | Condone all M marks for misread of both da                     | ays for any bar:              |  |  |  |
|      | Archery : 39 ÷ 3 = 13  | M1                            |  |  |  |
|      | Walking : 50 ÷ 5 = 10  |                               |  |  |  |
|      | Sailing : 34 ÷ 2 = 17 (Total = 40)                             | M1A0                          |  |  |  |
|      | NB 1 + 3 = 4 is M0   |                               |  |  |  |
|      | NB 1 + 5 = 6 is M0   |                               |  |  |  |
|      | $12 \div 3 + 30 \div 5 + 15 \div 2 = 4 + 6 + 8 = 18$ is M1M1A0 |                               |  |  |  |
|      | (the 8 is from wrong working but one misrea                    | d of a bar height is allowed) |  |  |  |

|   | Alternative method 1  |       |  |  |
|---|---|-------|--|--|
|   | 1200 – 970 or 230   | M1    |  |  |
|   | $\frac{\text{their } 230}{1200} \times 100 \text{ or } 19.1(6)$ | M1dep |  |  |
|   |   |       | SC2 for an answer of 80.8  |  |
| 5 | 19.2  | A1    | SC1 Any answer with at least 2 dp seen and correctly rounded to 1 dp                           |  |
| 5 | Alternative method 2  | •     |  |  |
|   | $\frac{970}{1200} \times 100$ or 80.83                          | M1    |  |  |
|   | 100 – their 80.83 or 19.1(6)                                    | M1dep |  |  |
|   | 19.2  | A1    | SC2 for an answer of 80.8 SC1 Any answer with at least 2 dp seen and correctly rounded to 1 dp |  |
|   |   |       |  |  |
| 6 | 11 chosen with no other number less than 11 chosen              | B1    |  |  |
|   | 4 × 10 or 40  | M1    |  |  |
|   | 23  | A1    | SC1 for 2 numbers with a total of 34   |  |

| 7(a) $\frac{\frac{2}{5}}{\frac{4}{7}}$ $\frac{\frac{3}{7}}{\frac{4}{7}}$ | B2 B1 at least one pair of branches correct |
|--|---|
|--|---|

| 7(b) | $\frac{2}{5} \times \frac{3}{7}$ | M1 | oe<br>May be seen on tree diagram |
|------|----------------------------------|----|-----------------------------------|
| 7(5) | <u>6</u><br>35                   | A1 | oe 0.17()                         |

### **Additional Guidance**

Condone further work involving adding extra probabilities for the M mark, eg

7(b)

P(black, orange) + P(orange, black) = 
$$\frac{2}{5} \times \frac{3}{7} + \frac{3}{7} \times \frac{2}{5}$$
  
or

P(black, orange) + P(white, orange) = 
$$\frac{2}{5} \times \frac{3}{7}$$
 +  $\frac{3}{5} \times \frac{3}{7}$ 

M1A0

|   | 680 or 120   | B1   |  |
|---|--|------|--|
| 8 | their 680 × 19.6(0) or 13 328<br>and<br>(800 – their 680) × 23 or 2760 | M1   | their 680 must be in the range [560, 710] Allow reversed values as a misread |
|   | 16 088   | A1ft | ft their 680 if in the range [640, 690]<br>SC2 17 992                        |

| A -I -I | :4:   | -10.   | .!      |
|---------|-------|--------|---------|
| Aaa     | ition | ıaı Gu | iidance |

The SC2 is for swapping the prices

Allow [640, 690] for M1A1ft as this interval contains all the likely scale misreads for reading off around 17 - 18 years age

If the student misreads the graph for 680, the following pairs are likely combinations for M1A1ft:

 $640, 160 \rightarrow £16 224$ 

 $650, 150 \rightarrow £16 190$ 

8

660, 140 → £16 156

690,  $110 \rightarrow £16054$ 

Allow [560, 710] for M1as this is [15, 20] years

The following pairs score M1 max:

 $580, 220 \rightarrow (£16428)$ 

620,  $180 \rightarrow (£16\ 292)$ 

700,  $100 \rightarrow (£16\ 020)$ 

|      | min = 9 <b>and</b> max = 30 on box plot                                       | B1 |  |
|------|---|----|--|
|      | median = 21   | B1 |  |
| 9(a) | LQ = 15 and UQ = 27   | B1 | Condone 15.5 and 26  |
|      | Correct structure – box with LQ,<br>median, UQ and whiskers to min and<br>max | Q1 | Strand (ii) Logical organised working Must have scored at least B1 |

|      | Additional Guidance  |    |  |  |  |
|------|--|----|--|--|--|
| 0(a) | Mark the box plot first (allow normal tolerance of ± ½ square on diagram)  Only consider working if measures are not obvious from box plot |    |  |  |  |
| 9(a) |  |    |  |  |  |
|      | If extra (or no) vertical line(s) for median, assume box ends are LQ and UQ  | Q0 |  |  |  |

| 9(b) | Yes Ben's median (24) is bigger than<br>Amy's median (21)<br>or<br>Yes and 24 and 21 | B1ft | ft their box plot values from (a) oe |  |
|------|--|------|--------------------------------------|--|
|------|--|------|--------------------------------------|--|

|      | their 27 – their 15 or 12<br>or<br>25 – 20 or 5 | M1   | Condone '20 to 25' or '15 to 27' for M1   |
|------|---|------|---|
| 9(c) | Yes and Ben's IQR is 5 and Amy's IQR is 12      | A1ft | ft their box plot values from (a)  Accept Yes and his IQR is smaller for M1A1  SC1ft No and their ranges are both the same (21) |

| 10 | $\frac{21}{100} \times 1.262 \times 10^{11}$ or<br>$26\ 502\ 000\ 000$ or $2.6502 \times 10^{10}$ or<br>or<br>$\frac{34}{100} \times 6.7 \times 10^{7}$ or<br>$22\ 780\ 000$ or $2.278 \times 10^{7}$<br>or<br>$(1.262 \times 10^{11}) \div (6.7 \times 10^{7})$ or<br>1883.() | M1    | oe<br>Digits 26 502 or 2278 or 1883 imply M1 |
|----|--|-------|--|
|    | their 26 502 000 000 ÷ their 22 780 000 or their 1883.() $\times \frac{21}{100}$ ÷ $\frac{34}{100}$  | M1dep | oe<br>Digits 1163 imply M2                   |
|    | 1163.38() or 1163 or<br>1163.4 or 1163.39 or 1.163() × 10 <sup>3</sup>   | A1    |  |

| Each group in the sample is in the same proportion (as the population)  Q1  Oe Must refer to the idea of proportion Strand (i) Vocabulary | 11(a) | • • | Q1 | ' ' |  |
|---|-------|-----|----|-----|--|
|---|-------|-----|----|-----|--|

|       | Additional Guidance   |                            |    |  |  |
|-------|---|----------------------------|----|--|--|
|       | Use of word proportion(al), ratio, relative is usually worth a mark |                            |    |  |  |
|       | The word 'fair' without reference to idea of p                      | roportionate is not enough |    |  |  |
|       | distributed equally between sections                                | В0                         |    |  |  |
|       | splitting the data fairly   | В0                         |    |  |  |
| 11(a) | grouped sample. Strata means group                                  | В0                         |    |  |  |
|       | in the same ratio as the whole group                                | B1                         |    |  |  |
|       | relative in size to the group                                       | B1                         |    |  |  |
|       | choosing fair proportions   | B1                         |    |  |  |
|       |   | B1                         |    |  |  |
|       | the same percentage of each group                                   |                            | B1 |  |  |

|       | $\frac{35}{35 + 220 + 45} \times 60$                                   | M1   | oe 35 ÷ 5  |
|-------|--|------|--|
|       | 7  | A1   | May be implied by $\frac{7}{60}$   |
| 11(b) | $\frac{\text{their 7}}{60} \text{ and } \frac{\text{their 7} - 1}{59}$ | M1   | Condone $\frac{\text{their 7}}{60} \times \frac{\text{their 7-1}}{60}$ or $\frac{\text{their 7}}{60} \times \frac{\text{their 7}}{59}$ or $\frac{35}{300} \times \frac{34}{299}$ |
|       | $\frac{42}{3540}$ or $\frac{7}{590}$ or 0.0118() or 0.0119 or 0.012    | A1ft | oe ft their $\frac{\text{their } 7}{60} \times \frac{\text{their } 7-1}{59}$ SC2 $\frac{119}{8970}$ or 0.013 oe  |

|       | Alternative method 1   |    |   |  |  |
|-------|--|----|---|--|--|
| 12(a) | $(175-170) \times 2$ or 10 (firefighters)<br>or $(185-175) \times 3.8$<br>or $(190-185) \times 6$<br>or $(200-190) \times 1.2$ or 12 | M1 |   |  |  |
|       | 38 or 30   | A1 |   |  |  |
|       | 175 ≤ height < 185 and 38 seen   | A1 | Working needed  SC1 for 175 ≤ height < 185 without relevant working  Condone 175 – 185 or 185 – 175 |  |  |
|       | Alternative method 2   |    |   |  |  |
|       | 170 to 175 = 2 or = 50<br>or 190 to 200 = 2.4 or = 60  | M1 | Counts squares  |  |  |
|       | 7.6 or 6<br>or<br>190 (firefighters) or 150  | A1 | Must be from counting squares   |  |  |
|       | 175 ≤ height < 185 and 190 seen<br>or<br>175 ≤ height < 185 and 7.6 seen   | A1 | Working needed  SC1 for 175 ≤ height < 185 without relevant working  Condone 175 – 185 or 185 – 175 |  |  |

| 12(a) | Additional Guidance   |  |  |  |
|-------|---|--|--|--|
|       | Ignore a slip in calculating the end bar(s) if middle correct |  |  |  |

|       | Alternative method 1   |        |   |  |  |
|-------|--|--------|---|--|--|
| 12(b) | Midpoints seen or implied 172.5, 180, 187.5, 195   | B1     | Condone one error   |  |  |
|       | their $\Sigma fx$<br>$10 \times 172.5 + 38 \times 180 + 30 \times 187.5 + 12 \times 195$<br>or $1725 + 6840 + 5625 + 2340$<br>or $16530$ | M1     | Condone one error ft their midpoints  |  |  |
|       | their $\Sigma fx \div 90$  | M1 dep | their 16 530 ÷ 90   |  |  |
|       | 184 or 183.7 or 183.66 or 183.67   | A1     | Anything less accurate than 2dp requires correct working seen  NB Using heights gives 183.69 and scores B1 only |  |  |
|       | Alternative method 2   |        |   |  |  |
|       | Midpoints seen or implied 172.5, 180, 187.5, 195   | B1     | Condone one error   |  |  |
|       | their $\Sigma fx$<br>2 × 172.5 + 7.6 × 180 + 6 × 187.5 +<br>2.4 × 195<br>or 345 + 1368 + 1125 + 468<br>or 3306                           | M1     | Condone one error ft their midpoints  |  |  |
|       | their $\Sigma fx \div 18$  | M1 dep | their 3306 ÷ 18   |  |  |
|       | 184 or 183.7 or 183.66 or 183.67   | A1     | Anything less accurate than 2dp requires correct working seen   |  |  |
|       |  |        | NB Using heights gives 183.69 and scores B1 only  |  |  |
| 12/h) | Additional Guidance  |        |   |  |  |
| 12(b) | A repeated consistent error is only one error  |        |   |  |  |
| 12(c) | One correct bound seen<br>170.35 or 170.45 or<br>195.55 or 195.65  | M1     | 195.6 – 170.4 + 0.1   |  |  |
|       | 25.3   | A1     |   |  |  |